Comparing observed and theoretical distributions

Maarten L. Buis

Institut für Soziologie Eberhard Karls Universität Tübingen www.maartenbuis.nl

Maarten L. Buis Comparing observed and theoretical distributions

<□> < □> < □> < □> = □ = のへへ

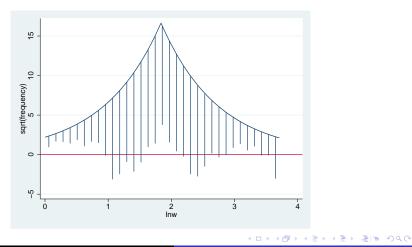
Univariate distributions Marginal distributions

Laplace distribution

```
. sysuse nlsw88, clear (NLSW, 1988 extract)
```

```
. gen lnw = ln(wage)
```

```
. hangroot lnw, dist(laplace)
(bin=33, start=.00493961, width=.11219493)
```



Maarten L. Buis Comparing observed and theoretical distributions

 Comparing the distribution of an observed variable with a theoretical distribution

◆□ ▶ ◆□ ▶ ◆ 三 ▶ ◆ □ ▶ ◆ □ ▶ ◆ □ ▶

- Comparing the distribution of an observed variable with a theoretical distribution
 - For example: the residuals after a linear regression should follow a normal/Gaussian distributed

▲□ > ▲ Ξ > ▲ Ξ > Ξ Ξ - 의 Q ()

- Comparing the distribution of an observed variable with a theoretical distribution
 - For example: the residuals after a linear regression should follow a normal/Gaussian distributed
- Two parts
 - Part 1 focusses on:
 - univariate distributions
 - hanging and suspended rootograms

▲□ → ▲ 三 → ▲ 三 → 三 三 → の < (~

- Comparing the distribution of an observed variable with a theoretical distribution
 - For example: the residuals after a linear regression should follow a normal/Gaussian distributed
- Two parts
 - Part 1 focusses on:
 - univariate distributions
 - hanging and suspended rootograms
 - Part 2 focusses on:
 - marginal distributions
 - hanging and suspend rootograms and pp and qq-plots

▲□ > ▲ Ξ > ▲ Ξ > Ξ Ξ - 의 Q ()

Univariate distributions Marginal distributions

Outline

Univariate distributions

Marginal distributions

Maarten L. Buis Comparing observed and theoretical distributions

histogram with normal curve

| • | sysuse | nlsw88, | clear |
|---|--------|---------|-------|
|---|--------|---------|-------|

- (NLSW, 1988 extract)
- . gen ln_w = ln(wage)
- . reg ln_w grade age ttl_exp tenure

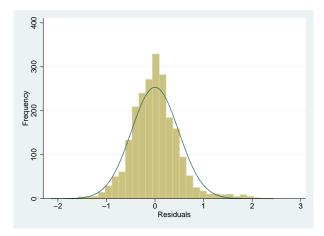
| Source | SS | df | | MS | | Number of obs F(4, 2224) Prob > F R-squared | = 2229 = 214.79 |
|--|--|---|-------------------|---|---|---|--|
| Model Residual | 203.980816 528.026987 | 4 2224 | | 952039 422206 | | | = 0.0000 = 0.2787 |
| Total | 732.007802 | 2228 | .328 | 549283 | | Adj R-squared Root MSE | = 0.2774 = .48726 |
| ln_w | Coef. | Std. | Err. | t | P> t | [95% Conf. | Interval] |
| grade age ttl_exp tenure _cons | .0798009 009702 .0312377 .0121393 .7426107 | .0041 .0034 .0027 .0022 .1447 | 036 926 939 | 19.09 -2.85 11.19 5.29 5.13 | 0.000 0.004 0.000 0.000 0.000 | .0716048 0163765 .0257613 .0076408 .4588348 | .087997 0030274 .0367141 .0166378 1.026387 |

. predict resid, resid (17 missing values generated) . hist resid, normal freg

(bin=33, start=-2.1347053, width=.13879342)

Univariate distributions Marginal distributions

histogram with normal curve



Maarten L. Buis Comparing observed and theoretical distributions

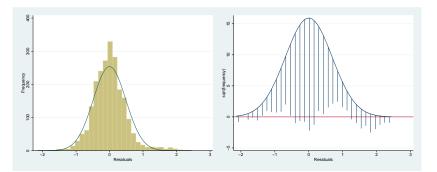
A B + A B +
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A

▲ 臣 ▶ ▲ 臣 ▶ 王 目 = り Q Q

Univariate distributions Marginal distributions

hanging rootogram, Tukey 1972 and 1977

. hangroot resid (bin=33, start=-2.1347053, width=.13879342)



Maarten L. Buis Comparing observed and theoretical distributions

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □

 For a histogram the variable is broken up in a number of bins.

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@

- For a histogram the variable is broken up in a number of bins.
- The hight of a bar/spike is the number of observations falling in a bin.

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@

- For a histogram the variable is broken up in a number of bins.
- The hight of a bar/spike is the number of observations falling in a bin.
- One can think of this number of observations as following a multinomial distribution.

<ロ> <同> <同> < 回> < 回> < 回> < 回</p>

- For a histogram the variable is broken up in a number of bins.
- The hight of a bar/spike is the number of observations falling in a bin.
- One can think of this number of observations as following a multinomial distribution.
- Confidence intervals for these counts are computed using Goodman's (1965) approximation of the simultaneous confidence interval.

▲□ > ▲ Ξ > ▲ Ξ > Ξ Ξ - 의 Q ()

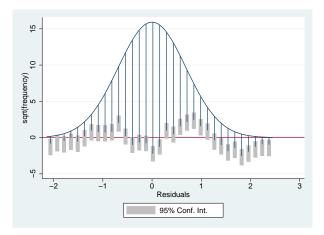
- For a histogram the variable is broken up in a number of bins.
- The hight of a bar/spike is the number of observations falling in a bin.
- One can think of this number of observations as following a multinomial distribution.
- Confidence intervals for these counts are computed using Goodman's (1965) approximation of the simultaneous confidence interval.
- For (hanging) rootograms these confidence intervals are transformed to the square root scale.

<□> < □> < □> < □> = □ = のへへ

- For a histogram the variable is broken up in a number of bins.
- The hight of a bar/spike is the number of observations falling in a bin.
- One can think of this number of observations as following a multinomial distribution.
- Confidence intervals for these counts are computed using Goodman's (1965) approximation of the simultaneous confidence interval.
- For (hanging) rootograms these confidence intervals are transformed to the square root scale.
- These confidence intervals do not take into account that:
 - the parameters of the theoretical curve are often estimated
 - and that nearby bins are often similar.

うから 正正 イヨト イヨト うらう

. hangroot resid, ci (bin=33, start=-2.1347053, width=.13879342)



Maarten L. Buis Comparing observed and theoretical distributions

 We know that the residuals should follow a normal distribution with mean 0 and standard deviation e (rmse).

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@

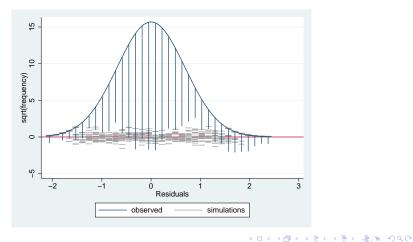
- We know that the residuals should follow a normal distribution with mean 0 and standard deviation e (rmse).
- We can compare the observed distribution with several draws from this theoretical distribution.

▲□ > ▲ Ξ > ▲ Ξ > Ξ Ξ - 의 Q ()

- We know that the residuals should follow a normal distribution with mean 0 and standard deviation e (rmse).
- We can compare the observed distribution with several draws from this theoretical distribution.
- The simulated distributions capture the variability one can expect if our model is true

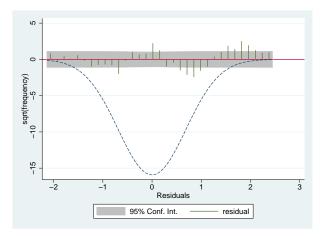
```
. forvalues i = 1/20 {
2. qui gen sim`i' = rnormal(0,`e(rmse)') if e(sample)
3. }
```

```
. hangroot resid, sims(sim*) jitter(5)
(bin=34, start=-2.1347053, width=.13471126)
```



Suspended rootogram

. hangroot resid, ci susp theoropt(lpattern(-))
(bin=33, start=-2.1347053, width=.13879342)



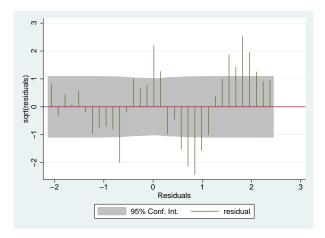
Maarten L. Buis Comparing observed and theoretical distributions

A B + A B +
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A
 A

★ E ► ★ E ► E = 9 Q Q

Suspended rootogram

. hangroot resid, ci susp notheor (bin=33, start=-2.1347053, width=.13879342)



Maarten L. Buis Comparing observed and theoretical distributions

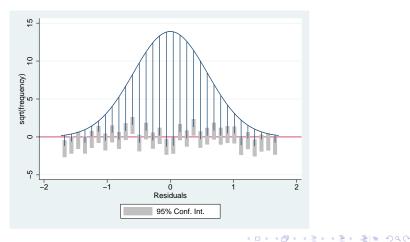
Univariate distributions Marginal distributions

Aside: Where did that bi-modality come from?

. qui reg ln_w grade age ttl_exp tenure union

```
. predict resid2, resid
(380 missing values generated)
```

```
. hangroot resid2, ci
(bin=32, start=-1.7272859, width=.10744561)
```



Maarten L. Buis Comparing observed and theoretical distributions

Where did the parameters come from?

► By default hangroot tries to estimate those parameters.

<□> < □> < □> < □> = □ = のへへ

Where did the parameters come from?

- ► By default hangroot tries to estimate those parameters.
- One can directly specify the parameters using the par() option. In this case one would type:

hangroot resid, par(0 'e(rmse)')

▲□ > ▲ Ξ > ▲ Ξ > Ξ Ξ - 의۹ @

Where did the parameters come from?

- By default hangroot tries to estimate those parameters.
- One can directly specify the parameters using the par() option. In this case one would type: hangroot resid, par(0 `e(rmse)')
- One can first use an estimation command to estimate the parameters. In this case one would type: regres resid

hangroot

▲□ → ▲ 三 → ▲ 三 → 三 三 → の へ ()

Is this just for the normal distribution?

One can specify other distributions with the dist() option.

| 1 2 | |
|-------------------------|---------------------------------|
| normal / Gaussian | Singh-Maddala |
| lognormal | Generalized Beta II |
| logistic | generalized extreme value |
| Weibull | exponential |
| Chi square | Laplace |
| gamma | uniform |
| Gumbel | geometric |
| inverse gamma | Poisson |
| Wald / inverse Gaussian | zero inflated Poisson |
| beta | negative binomial I |
| Pareto | negative binomial II |
| Fisk / log-logistic | zero inflated negative binomial |
| Dagum | |

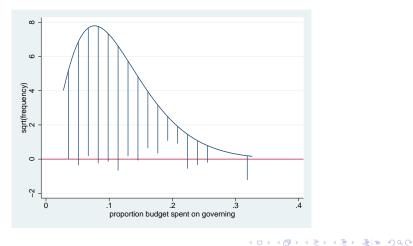
▲□ → ▲ 三 → ▲ 三 → 三 三 → の へ ()

Univariate distributions Marginal distributions

Other examples: a beta distribution

. use "`home'\citybudget", clear (Spending on different categories by Dutch cities in 2005)

. hangroot governing, dist(beta) (bin=19, start=.02759536, width=.01572787)

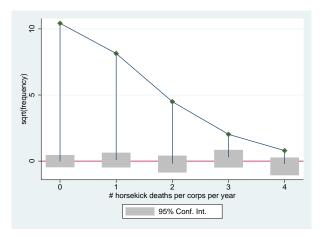


Maarten L. Buis Comparing observed and theoretical distributions

Univariate distributions Marginal distributions

Other examples: a Poisson distribution

. use "`home'\cavalry", clear (horsekick deaths in 14 Prussian cavalry units 1875-1894) . hangroot deaths [fw=freq], ci dist(poisson) (start=0, width=1)



Maarten L. Buis Comparing observed and theoretical distributions

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@

```
. program drop all
. program define sim, rclass
 1.
            drop all
  2.
            set obs 250
 3
            gen x1 = rnormal()
 4.
            gen x^2 = rnormal()
  5.
            gen x3 = rnormal()
 6.
            gen y = runiform() < invlogit(-2 + x1)
 7
            logit v x1 x2 x3
 8
            test x2=x3=0
 9.
            return scalar p_250 = r(p)
            return scalar chi2 250 = r(chi2)
 10.
             logit y x1 x2 x3 in 1/25
            test x2=x3=0
 13.
             return scalar p_25 = r(p)
 14.
             return scalar chi2 25 = r(chi2)
 15.
. end
. set seed 123456
. simulate chi2 250=r(chi2 250) p 250=r(p 250) ///
          chi2_25 =r(chi2_25) p_25 =r(p_25) , ///
          reps(1000) nodots : sim
      command: sim
    chi2_250: r(chi2_250)
       p 250: r(p 250)
     chi2 25: r(chi2 25)
        p 25: r(p 25)
```

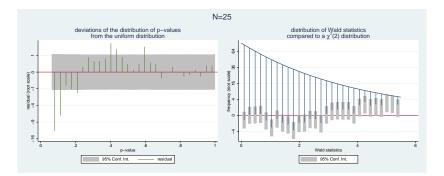
<ロ> <同> <同> < 三> < 三> < 三> 三日 のQ()

```
. hangroot chi2 25, dist(chi2) par(2) name(chi, replace) ci
5
               title("distribution of Wald statistics"
                     "compared to a {&chi}{sup:2}(2) distribution" ) ///
               xtitle(Wald statistics)
>
              ytitle("frequency (root scale)")
              ylab(-2 "-4" 0 "0" 2 "4" 4 "16" 6 "36" 8 "64")
>
(bin=29, start=.00226492, width=.18900082)
 hangroot p 25 , dist(uniform) par(0 1)
               susp notheor ci name (p, replace)
>
               title ("deviations of the distribution of p-values"
                     "from the uniform distribution")
               xtitle("p-value") vtitle("residual (root scale)")
              ylab(-4 "-16" -3 "-9" -2 "-4" -1 "-1" 0 "0" 1 "1")
>
(bin=29, start=.06446426, width=.03222082)
```

<ロ> <同> <同> < 回> < 回> < 回> < 回</p>

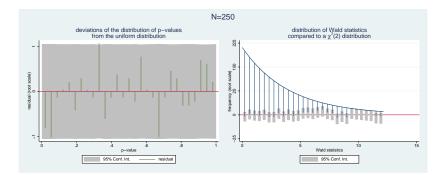
```
. hangroot chi2_250, dist(chi2) par(2) name(chi2, replace) ci
>
               title("distribution of Wald statistics"
                     "compared to a {&chi}{sup:2}(2) distribution" ) ///
               xtitle(Wald statistics)
>
               ytitle("frequency (root scale)")
               ylab(-5 "-25" 0 "0" 5 "25" 10 "100" 15 "225" )
>
(bin=29, start=.00158109, width=.41837189)
 hangroot p 250 , dist(uniform) par(0 1)
               susp notheor ci name (p2, replace)
>
               title ("deviations of the distribution of p-values"
                     "from the uniform distribution")
               xtitle("p-value") vtitle("residual (root scale)")
>
               ylab(-1 0 1)
(bin=29, start=.00231769, width=.03437559)
```

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへの



Maarten L. Buis Comparing observed and theoretical distributions

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@



Maarten L. Buis Comparing observed and theoretical distributions

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□□ のQ@

Outline

Univariate distributions

Marginal distributions

Maarten L. Buis Comparing observed and theoretical distributions

marginal distribution

In linear regression the residuals have a known theoretical distribution: normal/Gaussian distribution.

▲□ ▶ ▲ 臣 ▶ ▲ 臣 ▶ 三 臣 ● の Q @

marginal distribution

- In linear regression the residuals have a known theoretical distribution: normal/Gaussian distribution.
- This is typically not the case in other models like Poisson regression or beta regression.

marginal distribution

- In linear regression the residuals have a known theoretical distribution: normal/Gaussian distribution.
- This is typically not the case in other models like Poisson regression or beta regression.
- The theoretical marginal distribution of the dependent variable is known: It is a mixture distribution where each observation gets its own parameters

◎ ▶ ▲ 三 ▶ ▲ 三 ▶ 三 三 ● ○ ○ ○

Marginal distribution is a mixture distribution

. set seed 1234

. drop _all

. set obs 1000

obs was 0, now 1000

. gen byte x = _n <= 250

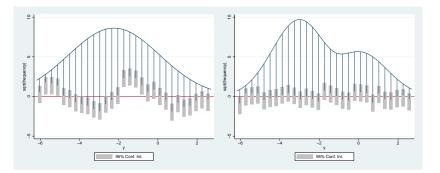
. gen y = -3 + 3 + x + rnormal()

Marginal distribution is a mixture distribution

. hangroot y, dist(normal) ci name(wrong, replace)
(bin=29, start=-6.1794977, width=.30656038)

. qui reg y x

. hangroot, ci name(right, replace)
(bin=29, start=-6.1794977, width=.30656038)



Maarten L. Buis Comparing observed and theoretical distributions

◆□ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶

comparing fit of count models (Poisson)

```
. use "`home'\couart2", clear
(Academic Biochemists / S Long)
. gen lnment = ln(ment)
(90 missing values generated)
. gui poisson art fem mar kid5 phd lnment
. predict lambda, n
(90 missing values generated)
. forvalues i=1/20 {
            qui gen sim`i' = rpoisson(lambda)
 2.
 3. }
. hangroot , sims(sim*) jitter(5) susp notheor ///
            title (poisson) name (poiss, replace) ///
>
>
                     legend(off)
(start=0, width=1)
```

also see: Hilbe 2010

<ロ> <同> <同> < 三> < 三> < 三> 三日 のQ()

comparing fit of count models (zero inflated Poisson)

```
. use "`home'\couart2", clear
(Academic Biochemists / S Long)
. gen lnment = ln(ment)
(90 missing values generated)
. gui zip art fem mar kid5 phd lnment, inflate( cons)
. predict lambda, xb
(90 missing values generated)
. replace lambda = exp(lambda)
(825 real changes made)
. predict pr, pr
. forvalues i=1/20 {
             qui gen sim`i' = cond(runiform() < pr, 0, rpoisson(lambda))</pre>
 2.
 3. }
. hangroot , sims(sim*) jitter(5) susp notheor ///
>
             title(zip) name(zip, replace)
>
                     legend(off)
(start=0, width=1)
```

<ロ> <同> <同> < 三> < 三> < 三> 三日 のQ()

comparing fit of count models (negative binomial)

```
. use "`home'\couart2", clear
(Academic Biochemists / S Long)
. gen lnment = ln(ment)
(90 missing values generated)
. gui nbreg art fem mar kid5 phd lnment
. predict xb, xb
(90 missing values generated)
. tempname a ia
. scalar `a' = e(alpha)
. scalar ia' = 1/a'
. gen exb = exp(xb)
(90 missing values generated)
. gen xg = .
(915 missing values generated)
. gen xbg = .
(915 missing values generated)
. forvalues i = 1/20 {
  2.
     qui replace xg = rgamma(`ia', `a')
 3
            qui replace xbg = exb*xg
            qui generate sim`i' = rpoisson(xbg)
 4.
 5. }
. hangroot , sims(sim*) jitter(5) susp notheor ///
>
            title(neg. binomial)
>
                     legend(off) name(nb, replace)
(start=0, width=1)
```

also see: Hilbe 2010

<ロ> <同> <同> < 回> < 回> < 回> < 回</p>

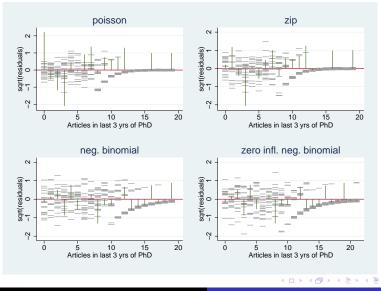
comparing fit of count models (zero inflated negative binomial)

```
. use "`home'\couart2", clear
(Academic Biochemists / S Long)
. gen lnment = ln(ment)
(90 missing values generated)
. qui zinb art fem mar kid5 phd lnment, inflate( cons)
. predict xb, xb
(90 missing values generated)
. predict pr, pr
. tempname a ia
. scalar `a' = exp([lnalpha] b[ cons])
. scalar `ia' = 1/`a'
den exb = exp(xb)
(90 missing values generated)
. gen xg = .
(915 missing values generated)
. gen xbg = .
(915 missing values generated)
. forvalues i = 1/20 {
 2.
            qui replace xq = rqamma(`ia', `a')
  3.
             qui replace xbg = exb*xg
 4.
             qui generate sim`i' = cond(runiform() < pr. 0, rpoisson(xbg))
 5. }
. hangroot , sims(sim*) jitter(5) susp notheor ///
>
            title(zero infl. neg. binomial) ///
                     name(znb, replace) legend(off)
(start=0, width=1)
```

<ロ> <同> <同> < 回> < 回> < 回> < 回</p>

Univariate distributions Marginal distributions

comparing fit of count models



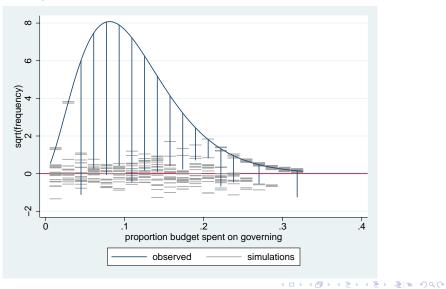
Maarten L. Buis Comparing observed and theoretical distributions

ELE DQC

Beta regression

```
. use "`home `\citybudget", clear
(Spending on different categories by Dutch cities in 2005)
. qui betafit governing, mu(noleft minorityleft popdens houseval)
. predict a, alpha
(1 missing value generated)
. predict b, beta
(1 missing value generated)
. forvalues i = 1/20 {
 2. qui gen sim'i' = rbeta(a,b)
 3. }
.
hangroot, sims(sim*) jitter(5)
(bin=20, start=.00440596, width=.01610095)
```

Beta regression

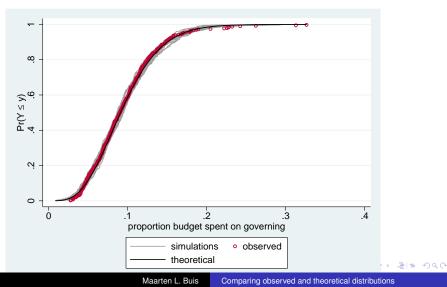


Maarten L. Buis Comparing observed and theoretical distributions

Univariate distributions Marginal distributions

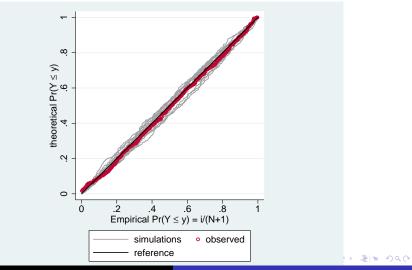
Cumulative density function

. margdistfit, cumul



PP-plot

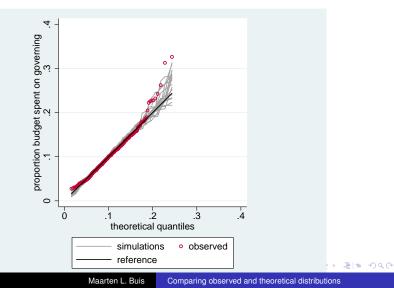
. margdistfit, pp



Maarten L. Buis Comparing observed and theoretical distributions

QQ-plot

. margdistfit, qq



 Deviations from the theoretical distribution are best shown as deviations from a straight line rather than a curve

▲ Ξ ▶ ▲ Ξ ▶ Ξ ΙΞ · · · · Q @

- Deviations from the theoretical distribution are best shown as deviations from a straight line rather than a curve
- Hanging and suspended rootograms are easy because many have been trained to look at histograms, but they require binning

▶ ★ Ξ ▶ ★ Ξ ▶ Ξ Ξ = 𝒴 𝔅

- Deviations from the theoretical distribution are best shown as deviations from a straight line rather than a curve
- Hanging and suspended rootograms are easy because many have been trained to look at histograms, but they require binning
- QQ and PP-plots allow you to see the raw data but many have not been trained to interpret them.

同 ト イヨ ト イヨ ト 三 日 つくつ

- Deviations from the theoretical distribution are best shown as deviations from a straight line rather than a curve
- Hanging and suspended rootograms are easy because many have been trained to look at histograms, but they require binning
- QQ and PP-plots allow you to see the raw data but many have not been trained to interpret them.
- One can derive the theoretical distribution implied by a regression type model by treating that distribution as a mixture distribution where each observations gets its own parameters.

<□> < □> < □> < □> 三目目 のQ()

- Deviations from the theoretical distribution are best shown as deviations from a straight line rather than a curve
- Hanging and suspended rootograms are easy because many have been trained to look at histograms, but they require binning
- QQ and PP-plots allow you to see the raw data but many have not been trained to interpret them.
- One can derive the theoretical distribution implied by a regression type model by treating that distribution as a mixture distribution where each observations gets its own parameters.
- One can get a feel for the amount of 'legitimate' variability by either plotting confidence intervals or random draws from the theoretical distribution.

References



Goodman, Leo A.

On Simultaneous Confidence Intervals for Multinomial Proportions. *Technometrics*, 7(2):247–254, 1965.



Hilbe, Joseph M.

Creating synthetic discrete-response regression models *The Stata Journal*, 10(1):104–124, 2010.



Tukey, John W.

Some Graphic and Semigraphic Displays.

in: T.A. Bancroft and S.A. Brown, eds., Statistical Papers in Honor of George W. Snedecor. Ames, Iowa: The Iowa State University Press, pp 293-316, 1972.



Tukey, John W.

Exploratory Data Analysis, Addison-Wesley, 1977.

◆□ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶