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**stintcox postestimation** — Postestimation tools for stintcox

Postestimation commands predict margins Remarks and examples Methods and formulas References Also see

## **Postestimation commands**

The following postestimation commands are of special interest after stintcox:

Command	Description
estat gofplot	produce goodness-of-fit plot
stcurve	plot the survivor, failure, hazard, or cumulative hazard function
stintcoxnp	plot nonparametric curves and Cox predicted curves
stintphplot	plot $-\ln\{-\ln(\text{survival})\}\ \text{curves}$

The following standard postestimation commands are also available:

Command	Description
contrast	contrasts and ANOVA-style joint tests of estimates
estat ic	Akaike's, consistent Akaike's, corrected Akaike's, and Schwarz's Bayesian information criteria (AIC, CAIC, AICc, and BIC)
estat summarize	summary statistics for the estimation sample
estat vce	variance-covariance matrix of the estimators (VCE)
estimates	cataloging estimation results
etable	table of estimation results
hausman	Hausman's specification test
lincom	point estimates, standard errors, testing, and inference for linear combinations of coefficients
lrtest	likelihood-ratio test
margins	marginal means, predictive margins, marginal effects, and average marginal effects
marginsplot	graph the results from margins (profile plots, interaction plots, etc.)
nlcom	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients
predict	hazard ratios, survivor functions, influence statistics, residuals, etc.
predictnl	point estimates, standard errors, testing, and inference for generalized predictions
pwcompare	pairwise comparisons of estimates
test	Wald tests of simple and composite linear hypotheses
testnl	Wald tests of nonlinear hypotheses

# predict

#### **Description for predict**

predict creates new variables containing predictions such as hazard ratios, linear predictions, standard errors, and baseline survivor and baseline cumulative hazard functions.

#### Menu for predict

Statistics > Postestimation

#### Syntax for predict

```
Single-record-per-subject interval-censored data with baseline covariates
```

```
 \begin{array}{c} \texttt{predict} \; \left[ \textit{type} \right] \; \textit{newvar} \; \left[ \textit{if} \right] \; \left[ \textit{in} \right] \; \left[ \; , \; \textit{statistic} \right] \\ \\ \texttt{predict} \; \left[ \textit{type} \right] \; \left\{ \; \textit{stub*} \; | \; \textit{newvar}_l \; \; \textit{newvar}_u \; \right\} \; \left[ \textit{if} \; \right] \; \left[ \; \textit{in} \; \right] \; , \; \textit{statistic2} \\ \end{aligned}
```

Single-record-per-subject interval-censored data with time-varying covariates

```
predict [type] newvar [if] [in] [, mgale]
predict [type] { stub* | newvar_l | newvar_u } [if] [in] [, statistic | statistic2]
```

Multiple-record-per-subject interval-censored data

```
predict [type] newvar [if] [in] [, statistic statistic2]
```

For single-record-per-subject data, predictions that depend on time, statistic2, are calculated for both the lower endpoint  $t_l$  and the upper endpoint  $t_u$  of the time interval specified in stintcox's interval() option and thus are stored in two new variables. This also applies to each statistic except mgale in the presence of time-varying covariates. For multiple-record-per-subject data, predictions are calculated for the examination times specified in stintcox's time() option and are always stored in a single variable.

statistic Description					
Main					
hr	predicted hazard ratio, also known as the relative hazard; the default				
хb	linear prediction $\mathbf{x}_i \widehat{\boldsymbol{\beta}}$				
stdp	standard error of the linear prediction, $SE(\mathbf{x}_i\widehat{\boldsymbol{\beta}})$				
* <u>mg</u> ale martingale-like residuals					
statistic2	Description				
Main					
*basesurv	baseline survivor function				
* basechazard	baseline cumulative hazard function				
* basehc	baseline hazard contributions				
*csnell	Cox-Snell-like residuals				

Unstarred statistics are available both in and out of sample; type predict ... if e(sample) ... if wanted only for the estimation sample. Starred statistics are calculated only for the estimation sample.

#### Options for predict

Main

hr, the default, calculates the relative hazard (hazard ratio), that is, the exponentiated linear prediction,  $\exp(\mathbf{x}_{j}\widehat{\boldsymbol{\beta}})$ . After stintcox with option tvc(), it calculates  $\exp\{\mathbf{x}_{j}\widehat{\boldsymbol{\beta}}+g(t)\mathbf{z}_{j}\widehat{\boldsymbol{\gamma}}\}\$ , where g(t) is a function of time as specified in stintcox's texp() option.

xb calculates the linear prediction from the fitted model. That is, you fit the model by estimating a set of parameters,  $\beta_1$ ,  $\beta_2$ , ...,  $\beta_p$ , and the linear prediction is  $\hat{\beta}_1 x_{1j} + \hat{\beta}_2 x_{2j} + \cdots + \hat{\beta}_p x_{pj}$ , often written in matrix notation as  $\mathbf{x}_i \hat{\boldsymbol{\beta}}$ .

The  $x_{1j}, x_{2j}, \ldots, x_{pj}$  used in the calculation are obtained from the data currently in memory and need not correspond to the data on the independent variables used in estimating  $\beta$ .

After stintcox with option tvc(), it calculates  $\mathbf{x}_j \hat{\boldsymbol{\beta}} + g(t) \mathbf{z}_j \hat{\boldsymbol{\gamma}}$ , where g(t) is a function of time as specified in stintcox's texp() option.

stdp calculates the standard error of the linear prediction xb.

basesury calculates the baseline survivor function.

basechazard calculates the baseline cumulative hazard.

basehc calculates the baseline hazard contributions.

mgale calculates interval-censored martingale-like residuals, which are an interval-censored version of martingale residuals for right-censored data.

csnell calculates the Cox-Snell-like residuals, which are the estimates of the cumulative hazard function obtained from the fitted model.

### margins

#### **Description for margins**

margins estimates margins of response for hazard ratios and linear predictions.

#### Menu for margins

Statistics > Postestimation

#### Syntax for margins

csnell

```
margins [marginlist] [, options]
  margins [marginlist], predict(statistic ...) [predict(statistic ...) ...] [options]
statistic
                   Description
hr
                   hazard ratio, also known as the relative hazard
xb
                   linear prediction
stdp
                   not allowed with margins
                   not allowed with margins
basesurv
                   not allowed with margins
basechazard
basehc
                   not allowed with margins
                   not allowed with margins
mgale
```

Statistics not allowed with margins are functions of stochastic quantities other than e(b).

For the full syntax, see [R] margins.

### Remarks and examples

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Remarks are presented under the following headings:

not allowed with margins

Baseline functions
Residuals and diagnostic measures
Postestimation after stintcox with option tvc()
Survivor curves for multiple-record-per-subject data with time-varying covariates

#### **Baseline functions**

predict after stintcox is used to generate a new variable or variables containing predicted values or residuals. predict can generate predicted hazard ratios, linear predictions, and standard errors of the linear predictions. It can also predict the baseline survivor function, baseline cumulative hazard function, or baseline hazard contributions. Baseline functions refer to the values of the functions when all covariates are set to 0. If the dataset is single-record-per-subject data, it calculates those statistics for both interval endpoints  $t_l$  and  $t_u$  specified in the interval() option with stintcox.

#### Example 1: Baseline survivor function

We use data from example 1 of [ST] stintcox and fit the Cox proportional hazards model in which the time to HIV infection depends on centered age variable (age\_mean) and whether a subject has been in jail at the time of recruitment (jail):

```
. use https://www.stata-press.com/data/r18/idu
(Modified Bangkok IDU Preparatory Study)
. stintcox age_mean i.jail, interval(ltime rtime)
note: using adaptive step size to compute derivatives.
Performing EM optimization (showing every 100 iterations):
Iteration 0: Log likelihood = -1086.2564
Iteration 100: Log likelihood = -600.55818
Iteration 200: Log likelihood = -600.47678
Iteration 295: Log likelihood = -600.46551
Computing standard errors: ..... done
Interval-censored Cox regression
                                                    Number of obs
                                                                     = 1,124
Baseline hazard: Reduced intervals
                                                           Uncensored =
                                                                              0
                                                        Left-censored =
                                                                             41
Event-time interval:
                                                        Right-censored =
                                                                            991
  Lower endpoint: ltime
                                                        Interval-cens. =
  Upper endpoint: rtime
                                                    Wald chi2(2)
                                                                       = 14.07
                                                    Prob > chi2
Log likelihood = -600.46551
                                                                       = 0.0009
                               NPG
                                                           [95% conf. interval]
               Haz. ratio
                            std. err.
                                           z
                                                P>|z|
                 .9647236
                            .0122201
                                        -2.84
                                                0.005
                                                           .9410676
                                                                       .9889743
    age_mean
        jail
        Yes
                 1.819721
                            .3804566
                                         2.86
                                                0.004
                                                           1.207927
                                                                       2.741379
```

Note: Standard error estimates may be more variable for small datasets and datasets with low proportions of interval-censored observations.

We can now estimate, for instance, the baseline survivor function. For this dataset, estimates of baseline survivor function, as well as baseline cumulative hazard and baseline hazard contributions, are intervals. So, to compute these statistics, we can either specify two new variable names with predict or specify a stub\* that will automatically create two new variable names stub1 and stub2; the first one will contain statistics computed using the lower time endpoint, and the second one will contain statistics computed using the upper time endpoint.

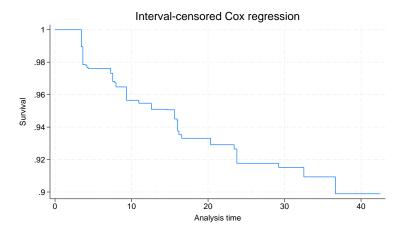
- . predict bs\_l bs\_u, basesurv
- . list bs\_l bs\_u ltime rtime age jail in 300/310

	bs_l	bs_u	ltime	rtime	age	jail
300. 301. 302. 303. 304.	.8989196 .9547279 .9647679 .8989196	0 .9450011 .9506636 0	40.00 11.97 8.20 39.93 39.48	15.84 15.18	36 21 36 40 25	Yes Yes Yes Yes Yes
305. 306. 307. 308. 309.	.8989196 .8989196 .9767599 .8989196	0 0 0 0	36.72 39.93 4.30 39.74 37.61		40 40 34 42 30	Yes Yes Yes No Yes
310.	.8989196	0	39.97	•	28	Yes

Listed above are the baseline survivor functions, bs\_1 and bs\_u, evaluated at the lower and upper time endpoints ltime and rtime, for subjects 300 to 310.

To graph the baseline survival curve, we can use stcurve with all covariates set to 0. We can also graph survivor functions after stintcox with covariates set to any value. See [ST] stcurve for more information.

. stcurve, survival at(age\_mean=0 jail=0)
note: function evaluated at specified values of selected covariates and
 overall means of other covariates (if any).



#### Residuals and diagnostic measures

For right-censored data, several types of residuals have been introduced to assess the appropriateness of the Cox proportional hazards model; see *Residuals and diagnostic measures* in [ST] **stcox postestimation** for details.

Farrington (2000) proposed extensions of those residuals for interval-censored data; see the reference for applications and a discussion of limitations of the residuals for interval-censored data. Here we offer martingale-like residuals and Cox-Snell-like residuals for visual model checking. Martingale-like residuals are useful in determining the functional form of covariates to be included in the model. They are also useful in assessing whether some covariates are needed in the model and for identifying outliers. Cox-Snell-like residuals are useful in assessing the overall model fit. If the model fits the data, those residuals should approximate an interval-censored sample from the standard exponential distribution. These residuals can be plotted by using estat gofplot.

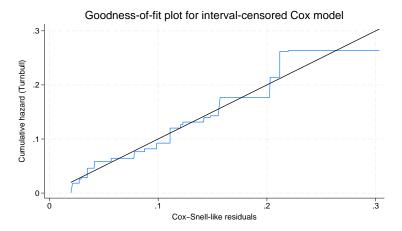
#### Example 2: Assess overall model fit

To visually assess the overall model fit, we can use the Cox-Snell-like residuals. For right-censored data, Cox and Snell (1968) argued that if the correct model has been fit to the data, these residuals should have a censored standard exponential distribution. With interval-censored, Cox-Snell-like residuals approximate an interval-censored sample from this distribution.

estat gofplot calculates an empirical estimate of the cumulative hazard function based on the Cox-Snell-like residuals and plots the resulting cumulative hazard rate against the residuals themselves. If the model fits the data, the plot is expected to approximate a straight line with slope 1.

Continuing with example 1, let's produce the goodness-of-fit plot.

. estat gofplot



The goodness-of-fit plot shows that the jagged line stays very close to the  $45^{\circ}$  reference line. The Cox proportional hazards model appears to fit the data well.

#### Example 3: Martingale-like residuals

Martingale-like residuals may be used as a diagnostic tool to assess the functional form of a covariate to be included in a Cox model. To find the appropriate functional form of a variable, we fit a Cox model without the variable of interest and then plot a lowess smooth of the martingale-like residuals against some transformation of that variable. If the transformation is appropriate, then the smooth should be approximately linear.

Continuing with example 1, we can apply this procedure to check whether the functional form of the covariate age\_mean is appropriate. First, we refit the Cox proportional hazards model on whether a subject has been in jail at the time of recruitment (jail). Then, we obtain the martingale-like residuals mg using predict with the mgale option. Last, we plot a lowess smooth of mg against variable age\_mean.

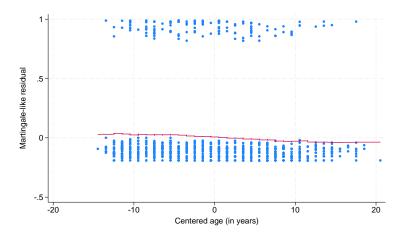
. stintcox i.jail, interval(ltime rtime) nolog note: using adaptive step size to compute derivatives.

Interval-censo	ored Cox regre	ession		Numbe	er of obs	=	1,124
Baseline hazar	rd: Reduced in	itervals			Uncensore	d =	0
				]	Left-censore	d =	41
Event-time int	terval:			R	ight-censore	d =	991
Lower endpoi	int: ltime			I	nterval-cens	. =	92
Upper endpoi	int: rtime						
				Wald	chi2(1)	=	6.24
Log likelihood	1 = -605.20197	•		Prob	> chi2	=	0.0125
		OPG					
	Haz. ratio	std. err.	z	P> z	[95% conf.	int	erval]

	Haz. ratio	OPG std. err.	z	P> z	[95% conf.	interval]
jail Yes	1.675924	. 3464929	2.50	0.013	1.11756	2.513264

Note: Standard error estimates may be more variable for small datasets and datasets with low proportions of interval-censored observations.

- . predict mg, mgale
- lowess mg age\_mean, mean noweight title("") note("") m(o)



We used the lowess command with the mean and noweight options to obtain a plot of the runningmean smoother to ease interpretation. The smooth appears nearly linear, supporting the inclusion of the untransformed version of age\_mean in our Cox model. Had the smooth not been linear, we would

1

have tried smoothing the martingale residuals against various transformations of age\_mean until we found one that produced a near-linear smooth.

#### Postestimation after stintcox with option tvc()

When the tvc() option is used with stintcox, the model includes the time-varying covariates formed by covariates in the tvc() option multiplied by the deterministic function of time specified in the texp() option. In this case, predictions that depend on the covariate pattern, such as a linear predictor and relative hazard, also depend on time. For instance, for single-record-per-subject data, predict, xb will now produce two new variables: one containing the linear predictor computed using the lower endpoint of the time interval and the other one computed using the upper endpoint.

After stintcox, tvc(), postestimation features such as predict and stcurve incorporate both fixed and time-varying covariates. For instance, the linear predictor will include the effects of both baseline covariates and time-varying covariates produced by the tvc() option.

Predictions of baseline functions and martingale-like residuals do not depend on covariates and are thus unaffected by stintcox, tvc().

#### Example 4: Predictions after stintcox with option tvc()

In Testing the proportional-hazards assumption using option tvc() in [ST] stintcox, we discovered that jail was one of the variables that did not satisfy the proportional-hazards assumption.

Let's fit the following model with a time-varying covariate  $\mathtt{jail} \times t$ :

$$h(t) = h_0(t) \exp{\{\beta_1 \times \text{age\_mean} + \beta_2 \times \text{jail} + \gamma_1 \times (\text{jail} \times t)\}}$$

We use the tvc() option to create the time-varying covariate jail  $\times t$ :

. stintcox age\_mean i.jail, interval(ltime rtime) tvc(i.jail) nohr note: using adaptive step size to compute derivatives.

Performing EM optimization (showing every 100 iterations):

Iteration 0: Log likelihood = -1086.2564
Iteration 100: Log likelihood = -597.6072
Iteration 200: Log likelihood = -597.52358
Iteration 295: Log likelihood = -597.51247

Computing standard errors: ..... done

Interval-censored Cox regression

Baseline hazard: Reduced intervals

Uncensored = 0

Left-censored = 41

Event-time interval:

Right-censored = 991

Event-time interval:
Lower endpoint: ltime
Upper endpoint: rtime

Wald chi2(3) = 16.87 Log likelihood = -597.51247 Prob > chi2 = 0.0008

		Coefficient	OPG std. err.	z	P> z	[95% conf.	interval]
mair	n age_mean	0360376	.0126271	-2.85	0.004	0607864	0112889
	jail Yes	1593675	.3777957	-0.42	0.673	8998335	.5810986
tvc	jail Yes	.0732193	.0342545	2.14	0.033	.0060818	.1403569

Notes: Standard error estimates may be more variable for small datasets and datasets with low proportions of interval-censored observations.

Variables in tvc equation interacted with \_t.

Wald test that [tvc] = 0: chi2(1) = 4.5690

Prob > chi2 = 0.0326

Interval-cens. =

92

Let's use predict, xb to calculate the linear prediction. Because the linear prediction now depends on time and there are two time interval endpoints in a single-record-per-subject data, predict requires two new variable names. Below, we use a stub notation xb\* that automatically creates two new variables, xb1 and xb2, to store linear predictions. To demonstrate, we list the results for subjects 30 and 95.

```
. predict xb*, xb
(991 missing values generated)
note: prediction includes time-varying covariates formed by stintcox, tvc().
```

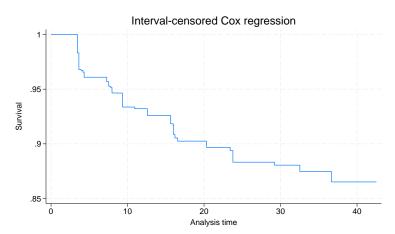
. list age\_mean jail ltime rtime xb1 xb2 if \_n==30 | \_n==95

	age_mean	jail	ltime rtime		il ltime rtime xb1		xb1	xb2
30.	.53825623	Yes	7.147541	13.213115	.3445733	.7886905		
95.	46174377	No	4.1311474	8.0327873		.0166402		

For subject 30, jail is equal to 1, and the linear predictions in xb1 are computed as  $\widehat{\beta}_1 \times \texttt{age\_mean} + \widehat{\beta}_2 + \widehat{\gamma}_1 \times \texttt{ltime}$  and in xb2 as  $\widehat{\beta}_1 \times \texttt{age\_mean} + \widehat{\beta}_2 + \widehat{\gamma}_1 \times \texttt{rtime}$ . For subject 95, jail = 0, and thus both x1 and x2 contain  $\widehat{\beta}_1 \times \texttt{age\_mean}$ .

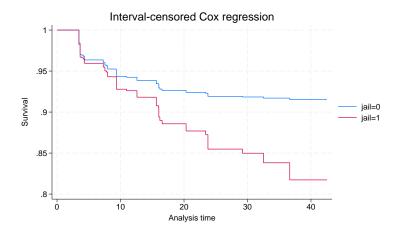
#### Example 5: stcurve after stintcox with option tvc()

stcurve can be used after stintcox to plot the estimated survivor, failure, hazard, or cumulative hazard function. When the tvc() option is specified with stintcox, stcurve incorporates the time-varying nature of the covariates. By default, a function is evaluated at the overall means of covariates in the model. For covariates specified in the tvc() option, their overall mean values are multiplied by the function of time, as specified in stintcox's texp() option, during a function evaluation.



Here jail is binary, so we may want to use the at() option to evaluate the survivor function for jail = 0 and jail = 1. The overall mean is used for any covariate not listed in at() (age\_mean in our example).

. stcurve, survival at(jail=(0 1))
note: function evaluated at specified values of selected covariates and
 overall means of other covariates (if any), multiplied by \_t for
 covariates in stintcox's tvc() option.



The survival of those who have not been imprisoned is higher than those who have.

#### 12

#### Survivor curves for multiple-record-per-subject data with time-varying covariates

By default, stcurve evaluates the survivor and other functions at the overall means of covariates. We can also use the at() option to evaluate functions at specific covariate values. Both of these options work well for baseline covariates. But multiple-record-per-subject data often include time-varying covariates. In that case, we may want to incorporate the time-varying nature of these covariates when plotting the survivor function or other functions. We can use the attmeans option to evaluate the function at time-specific means, which will vary with time for time-varying covariates. We can also specify our own time-varying values for all or some covariates by using the atframe() option.

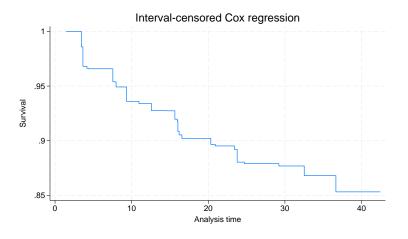
In general, care should be taken when interpreting the survivor function in the presence of time-varying covariates. The interpretation is valid only for external time-varying covariates, which are covariates that are external to an individual under study, such as air temperature. (Any covariate that is formed as an interaction of a baseline covariate and a deterministic function of time is an external covariate by construction.) For an internal time-varying covariate, which is generated by an individual in a study, such as wellness status, the survivor function is not well defined. See, for instance, Kalbfleisch and Prentice (2002) for details.

#### Example 6: stcurve with option attmeans

In example 4 in [ST] **stintcox**, we fit a model that included the time-varying <code>jail\_vary</code> variable. In this example, <code>jail\_vary</code> is an internal time-varying covariate because it can be observed for a subject only until a subject "survives" and is not censored. Although it would not be sensible to proceed with this example in practice, we will use it here solely to demonstrate the software.

So, continuing with example 4 in [ST] **stintcox**, after fitting the model with time-varying jail\_vary, we use stcurve with the attmeans option to plot the survivor curve that uses the time-specific mean values for covariates at each time point, hence accounting for the average changes of the covariates, specifically jail\_vary, over time:

```
. use https://www.stata-press.com/data/r18/idu2, clear
(Modified Bangkok IDU Preparatory Study with time-varying variable jail_vary)
. stintcox age_mean i.male i.needle i.inject i.jail_vary, id(id) time(time)
> status(is_seropos)
  (output omitted)
. stcurve, survival attmeans
note: function evaluated at time-specific means of covariates.
```



#### Example 7: stcurve with option atframe()

We can use the atframe() option to specify time-varying covariate values to be used to evaluate the survivor function. We first need to create a frame that includes all or a subset of the covariates and the time variable in your model and fill in those variables with the values we want to use for prediction and the corresponding time points. If a subset of the covariates is specified in atframe(), the unspecified covariates are evaluated, by default, at their overall means or, if the attmeans option is specified, at their time-specific means.

Suppose we want to plot the survivor curve for an individual with the same covariate pattern as subject 2 in our dataset. We start by creating a new frame called id2 and use frame put to copy the relevant information for subject 2 in this new frame. Then we list the data we just saved in frame id2.

- . frame put time age\_mean male needle inject jail\_vary if id==2, into(id2)
- . frame id2: list

	time	age_mean	male	needle	inject	jail_v~y
1.	4.1311475	-6.4617438	Yes	No	Yes	Yes
2.	8.2622951	-6.4617438	Yes	No	Yes	No
3.	12.295082	-6.4617438	Yes	No	Yes	No
4.	16.065574	-6.4617438	Yes	No	Yes	No
5.	20.098361	-6.4617438	Yes	No	Yes	No
6.	24.262295	-6.4617438	Yes	No	Yes	No

In frame id2, six examination times are recorded, and all covariate values for each examination time are filled in. Variables age\_mean, male, needle, and inject are constant, and variable jail\_vary changes at the second examination time.

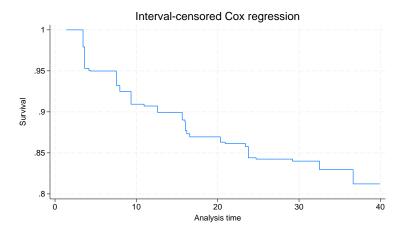
We can graph the survivor curve for this particular profile by typing

. stcurve, survival atframe(id2)

note: function evaluated at specified values of selected covariates and

overall means of other covariates (if any).

note: covariate values from frame id2 used to evaluate function.



Unless you provide covariate values for all distinct observed times used during estimation, stcurve will use the same imputation method as specified in the tvcovimpute() option with stintcox

([ST] stintcox) to impute the unobserved covariate values for time points that are not recorded in the frame.

1

#### Methods and formulas

Methods and formulas are presented under the following headings:

Predictions for single-record interval-censored data Predictions for multiple-record interval-censored data Survivor curves for interval-censored data

#### Predictions for single-record interval-censored data

For single-record interval-censored data, each subject i contains one observation  $(t_{li}, t_{ui}, \mathbf{x}_i)$ , where  $t_{li}$  and  $t_{ui}$  define the observed time interval and  $\mathbf{x}_i$  is a  $1 \times p$  vector of covariate values. Let  $\hat{\boldsymbol{\beta}}$  be a  $p \times 1$  vector of estimates of regression coefficients for  $\mathbf{x}_i$ .

Case of baseline covariates. The survivor function for subject i at time t can be estimated as

$$\widehat{S}_i(t) = \, \exp \big\{ \, - \!\! \sum_{t_k \le t} \widehat{h}_k \exp (\mathbf{x}_i \widehat{\boldsymbol{\beta}}) \big\}$$

where  $\hat{h}_k$   $(k=1,\ldots,m)$  are the estimates of the baseline hazard jumps at  $t_1,\ldots,t_m$  and  $t_1<\cdots< t_m$  are the distinct time points for all  $t_{li}>0$  and  $t_{ui}<\infty$ .

predict newvar, statistic may be used after stintcox to predict various quantities, according to each following statistic:

hr:

$$newvar_i = \exp(\mathbf{x}_i \hat{\boldsymbol{\beta}})$$

xb:

$$newvar_i = \mathbf{x}_i \widehat{\boldsymbol{\beta}}$$

stdp:

$$newvar_i = \widehat{se}(\mathbf{x}_i\widehat{\boldsymbol{\beta}})$$

mgale:

$$newvar_i = \frac{\widehat{S}_i(t_{li})\log\widehat{S}_i(t_{li}) - \widehat{S}_i(t_{ui})\log\widehat{S}_i(t_{ui})}{\widehat{S}_i(t_{li}) - \widehat{S}_i(t_{ui})}$$

For right-censored data, martingale residuals can be defined as the scores of the regression parameters. This property can carry over to the interval-censored data for martingale-like residuals mgale. Therefore, these residuals are expected to have mean zero and to be asymptotically uncorrelated. Furthermore, these residuals are orthogonal to variables included in the model. Thus, we can use them to assess the need to include other covariates in the model. See Farrington (2000) for details.

predict  $newvar_l$   $newvar_u$ , statistic may be used after stintcox to predict a pair of quantities for each observation for both the lower and upper endpoints of the time interval  $(t_{li}, t_{ui})$ , according to each following statistic:

basehc:

$$newvar_{li} = I(t_k = t_{li}) \widehat{h}_k$$
  $newvar_{ui} = I(t_k = t_{ui}) \widehat{h}_k$ 

basechazard:

$$newvar_{li} = \widehat{H}_0(t_{li}) = \sum_{k:t_k \le t_{li}} \widehat{h}_k$$
 
$$newvar_{ui} = \widehat{H}_0(t_{ui}) = \sum_{k:t_k \le t_{ui}} \widehat{h}_k$$

basesurv:

$$newvar_{li} = \widehat{S}_0(t_{li}) = \exp\left\{-\widehat{H}_0(t_{li})\right\}$$
 $newvar_{ui} = \widehat{S}_0(t_{ui}) = \exp\left\{-\widehat{H}_0(t_{ui})\right\}$ 

csnell:

$$newvar_{li} = -\log \widehat{S}_i(t_{li})$$
  
 $newvar_{ui} = -\log \widehat{S}_i(t_{ui})$ 

The Cox-Snell-like residuals are the estimates of the cumulative hazard function obtained from the fitted model. They are computed separately for each of the two interval endpoints. For interval-censored data, under the correct model assumption, these residuals are expected to approximate an interval-censored sample from the standard exponential distribution. Therefore, they can be used for checking the overall model fit. Cox-Snell-like residuals can never be negative and therefore are not symmetric about zero. See Farrington (2000) for details.

Case of time-varying covariates with option  $\mathbf{tvc}()$ . When the  $\mathbf{tvc}()$  option is specified with  $\mathbf{stintcox}$ , predict modifies its calculations so that they include the time-varying components. Let  $\mathbf{z}_i$  denote a  $1 \times q$  vector of covariates specified in the  $\mathbf{tvc}()$  option of  $\mathbf{stintcox}$ , and let g(t) denote the function of time specified in the  $\mathbf{texp}()$  option of  $\mathbf{stintcox}$ . Let a  $q \times 1$  vector  $\widehat{\gamma}$  contain the estimates of regression coefficients for  $\mathbf{z}_i$ . The survivor function for subject i at time t can be estimated as

$$\widehat{S}_i(t) = \exp\left[-\sum_{t_k \le t} \widehat{h}_k \exp\left\{\mathbf{x}_i \widehat{\boldsymbol{\beta}} + g(t_k) \mathbf{z}_i \widehat{\boldsymbol{\gamma}}\right\}\right]$$

Also, each following *statistic* changes to predict a pair of quantities for each observation for both the lower and upper endpoints of the time interval  $(t_{li}, t_{ui})$ :

hr:

$$newvar_{li} = \exp\{\mathbf{x}_i\widehat{\boldsymbol{\beta}} + g(t_{li})\mathbf{z}_i\widehat{\boldsymbol{\gamma}}\}$$

$$newvar_{ui} = \exp\{\mathbf{x}_i\widehat{\boldsymbol{\beta}} + g(t_{ui})\mathbf{z}_i\widehat{\boldsymbol{\gamma}}\}$$

xb:

$$newvar_{li} = \mathbf{x}_i \widehat{\boldsymbol{\beta}} + g(t_{li}) \mathbf{z}_i \widehat{\boldsymbol{\gamma}}$$
$$newvar_{ui} = \mathbf{x}_i \widehat{\boldsymbol{\beta}} + g(t_{ui}) \mathbf{z}_i \widehat{\boldsymbol{\gamma}}$$

stdp:

$$newvar_{li} = \widehat{\operatorname{se}} \left\{ \mathbf{x}_i \widehat{\boldsymbol{\beta}} + g(t_{li}) \mathbf{z}_i \widehat{\boldsymbol{\gamma}} \right\} = \left\{ \mathbf{x}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\beta}} \mathbf{x}_i' + 2g(t_{li}) \mathbf{z}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\beta}, \boldsymbol{\gamma}} \mathbf{x}_i' + g(t_{li})^2 \mathbf{z}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\gamma}} \mathbf{z}_i' \right\}^{\frac{1}{2}}$$

$$newvar_{li} = \widehat{\operatorname{se}} \left\{ \mathbf{x}_i \widehat{\boldsymbol{\beta}} + g(t_{ui}) \mathbf{z}_i \widehat{\boldsymbol{\gamma}} \right\} = \left\{ \mathbf{x}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\beta}} \mathbf{x}_i' + 2g(t_{ui}) \mathbf{z}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\beta}, \boldsymbol{\gamma}} \mathbf{x}_i' + g(t_{ui})^2 \mathbf{z}_i \widehat{\boldsymbol{\Sigma}}_{\boldsymbol{\gamma}} \mathbf{z}_i' \right\}^{\frac{1}{2}}$$

where  $\widehat{\Sigma}_{\beta}$  and  $\widehat{\Sigma}_{\gamma}$  are the estimated covariance matrices for  $\widehat{\beta}$  and  $\widehat{\gamma}$ , respectively, and  $\widehat{\Sigma}_{\beta,\gamma}$  is the estimated covariance matrix between  $\widehat{\beta}$  and  $\widehat{\gamma}$ .

#### Predictions for multiple-record interval-censored data

For multiple-record interval-censored data, subject  $i=1,\ldots,n$  may contain  $n_i$  observations. And each observation  $j=1,\ldots,n_i$  for subject i consists of  $(t_{ij},\delta_{ij},\mathbf{x}_{ij})$ , where  $t_{ij}$  is the examination time,  $\delta_{ij}$  denotes whether the event of interest occurs between  $t_{i(j-1)}$  and  $t_{ij}$  ( $t_{i(j-1)}=0$  if j=1), and  $\mathbf{x}_{ij}$  records covariate values at  $t_{ij}$ . Here  $\mathbf{x}_{ij}$  includes both baseline and time-varying covariates. For baseline covariates,  $\mathbf{x}_{ij}=\mathbf{x}_i$ . Without loss of generality, we assume that the examination times are sorted within the same subject. Let  $t_1<\cdots< t_m$  be the distinct observed time points for all  $t_{li}>0$  and  $t_{ui}<\infty$ , where  $t_{li}$  and  $t_{ui}$  define the observed time interval, based on  $(t_{ij},\delta_{ij})$ , that bracket the event of interest for subject i. The survivor function for subject i at the examination time  $t_{ij}$  can be estimated as

$$\widehat{S}_i(t_{ij}) = \, \exp \big\{ \, - \! \sum_{t_k \leq t_{ij}} \widehat{h}_k \exp(\mathbf{x}_{ik}^* \widehat{\boldsymbol{\beta}}) \big\}$$

where  $\hat{h}_k$   $(k=1,\ldots,m)$  are the estimates of the baseline hazard jumps at  $t_1,\ldots,t_m$  and  $\mathbf{x}_{ik}^*$  are the covariates' values for subject i at time  $t_k$ . For baseline covariates,  $\mathbf{x}_{ik}^* = \mathbf{x}_{ij} = \mathbf{x}_i$ . For time-varying covariates, if  $t_k$  happens to be  $t_{ij}$ , then  $\mathbf{x}_{ik}^* = \mathbf{x}_{ij}$ ; otherwise,  $\mathbf{x}_{ik}^*$  is imputed using the imputation rule specified in the tycovimpute() option of stintcox.

predict newvar, statistic may be used after stintcox to predict various quantities for each observation, according to each following statistic:

hr:

$$newvar_{ij} = \exp(\mathbf{x}_{ij}\widehat{\boldsymbol{\beta}})$$

xb:

$$newvar_{ij} = \mathbf{x}_{ij}\widehat{\boldsymbol{\beta}}$$

stdp:

$$newvar_{ij} = \widehat{se}(\mathbf{x}_{ij}\widehat{\boldsymbol{\beta}})$$

mgale:

$$newvar_{ij} = \frac{\widehat{S}_i(t_{i(j-1)})\log\widehat{S}_i(t_{i(j-1)}) - \widehat{S}_i(t_{ij})\log\widehat{S}_i(t_{ij})}{\widehat{S}_i(t_{i(j-1)}) - \widehat{S}_i(t_{ij})}$$

basehc:

$$newvar_{ij} = I(t_k = t_{ij})\hat{h}_k$$

basechazard:

$$\textit{newvar}_{ij} = \widehat{H}_0(t_{ij}) = \sum_{k: t_k \leq t_{ij}} \widehat{h}_k$$

basesurv:

$$newvar_{ij} = \widehat{S}_0(t_{ij}) = \exp\left\{-\widehat{H}_0(t_{ij})\right\}$$

csnell:

$$newvar_{ij} = -\log \widehat{S}_i(t_{ij})$$

When the tvc() option is specified with stintcox, predict computes the linear prediction xb as  $\mathbf{x}_{ij}\hat{\boldsymbol{\beta}} + g(t_{ij})\mathbf{z}_{ij}\hat{\boldsymbol{\gamma}}$  instead of  $\mathbf{x}_{ij}\hat{\boldsymbol{\beta}}$ . Here g(t) denotes the function of time specified in the texp() option of stintcox, and z denotes the covariates specified in the tvc() option of stintcox. The survivor function is then estimated as

$$\widehat{S}_i(t_{ij}) = \, \exp \Big[ \, - \!\! \sum_{t_k \leq t_{ij}} \widehat{h}_k \, \exp \big\{ \mathbf{x}_{ik}^* \widehat{\boldsymbol{\beta}} + g(t_k) \mathbf{z}_{ik}^* \widehat{\boldsymbol{\gamma}} \big\} \Big]$$

where  $\mathbf{z}_{ik}^*$  are defined similarly to  $\mathbf{x}_{ik}^*$  above but using the covariates  $\mathbf{z}_{ij}$ 's.

#### Survivor curves for interval-censored data

You can use the stcurve command to plot the survivor function after stintcox. stcurve can also plot the failure, hazard, or cumulative hazard function.

**Single-record interval-censored data.** By default, stcurve plots the estimated survivor function with covariates set to their mean values,

$$\widehat{S}(t) = \exp \left\{ -\sum_{t_k \le t} \widehat{h}_k \exp(\overline{\mathbf{x}} \widehat{\boldsymbol{\beta}}) \right\} = \widehat{S}_0(t) \exp(\overline{\mathbf{x}} \widehat{\boldsymbol{\beta}})$$

where  $\overline{\mathbf{x}}$  is a  $1 \times p$  mean vector of  $\mathbf{x}$ . When the tvc() option is specified with stintcox, the plotted survivor function becomes

$$\widehat{S}(t) = \exp \Big[ - \!\!\! \sum_{t_k \leq t} \widehat{h}_k \exp \big\{ \overline{\mathbf{x}} \widehat{\boldsymbol{\beta}} + g(t_k) \overline{\mathbf{z}} \widehat{\boldsymbol{\gamma}} \big\} \Big]$$

where  $\overline{\mathbf{z}}$  is a  $1 \times q$  mean vector of  $\mathbf{z}$ . Alternatively, you can specify your own values in stcurve's at() option. For covariates that are not specified in the at() option, the mean values are used. For details about the at() option, see Syntax of at() in [ST]  $adjustfor\_option$ .

**Multiple-record interval-censored data.** By default, stcurve plots the estimated survivor function with covariates set to their overall mean values:

$$\widehat{S}(t) = \exp \big\{ - \!\!\! \sum_{t_k \leq t} \widehat{h}_k \exp(\overline{\mathbf{x}} \widehat{\boldsymbol{\beta}}) \big\} = \widehat{S}_0(t) \operatorname{exp}(\overline{\mathbf{x}} \widehat{\boldsymbol{\beta}})$$

And with the tvc() option of stintcox, the estimated survivor function is computed by default as

$$\widehat{S}(t) = \, \exp \big[ \, - \!\! \sum_{t_k \leq t} \widehat{h}_k \exp \{ \overline{\mathbf{x}} \widehat{\boldsymbol{\beta}} + g(t_k) \overline{\mathbf{z}} \widehat{\boldsymbol{\gamma}} \} \big]$$

Let  $\overline{\mathbf{x}}_{t_k}$  be a  $1 \times p$  mean vector of  $\mathbf{x}_{ik}^*$  over all subjects at time  $t_k$  and  $\overline{\mathbf{z}}_{t_k}$  be a  $1 \times q$  mean vector of  $\mathbf{z}_{ik}^*$  over all subjects at time  $t_k$  (if the tvc() option is specified with stintcox). When the attmeans option is specified, stcurve plots the following estimated survivor function:

$$\widehat{S}(t) = \exp \left[ -\sum_{t_k \le t} \widehat{h}_k \exp \left\{ \overline{\mathbf{x}}_{t_k} \widehat{\boldsymbol{\beta}} + g(t_k) \overline{\mathbf{z}}_{t_k} \widehat{\boldsymbol{\gamma}} \right\} \right]$$

If stcurve's atframe() option is specified,  $\overline{\mathbf{x}}_{t_k}$  and  $\overline{\mathbf{z}}_{t_k}$  in the above will be replaced with  $\mathbf{x}_{t_k}^{\mathrm{new}}$  and  $\mathbf{z}_{t_k}^{\mathrm{new}}$ , where  $\mathbf{x}_{t_k}^{\mathrm{new}}$  are user-specified values if time  $t_k$  and the corresponding covariate values are recorded in the frame. Otherwise,  $\mathbf{x}_{t_k}^{\mathrm{new}}$  and  $\mathbf{z}_{t_k}^{\mathrm{new}}$  are imputed using the imputation rule specified in the tvcovimpute() option of stintcox. Then the survivor function can be estimated as

$$\widehat{S}(t) = \exp \left[ -\sum_{t_k < t} \widehat{h}_k \exp \left\{ \mathbf{x}_{t_k}^{\text{new}} \widehat{\boldsymbol{\beta}} + g(t_k) \mathbf{z}_{t_k}^{\text{new}} \widehat{\boldsymbol{\gamma}} \right\} \right]$$

The failure, hazard, and cumulative hazard functions are calculated based on the survivor function above.

#### References

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#### Also see

- [ST] **stintcox** Cox proportional hazards model for interval-censored survival-time data
- [ST] stintcox PH-assumption plots Plots of proportional-hazards assumption after stintcox
- [ST] stcurve Plot the survivor or related function after streg, stcox, and more
- [U] 20 Estimation and postestimation commands

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