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bitest — Binomial probability test

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Description

bitest performs exact hypothesis tests for binomial random variables. The null hypothesis is that the probability of a success on a trial is $\#_p$. The total number of trials is the number of nonmissing values of *varname* (in bitest) or $\#_N$ (in bitesti). The number of observed successes is the number of 1s in *varname* (in bitest) or $\#_{\text{succ}}$ (in bitesti). *varname* must contain only 0s, 1s, and missing.

bitesti is the immediate form of bitest; see [U] 19 Immediate commands for a general introduction to immediate commands.

Quick start

Exact test for probability of success (a = 1) is 0.4

bitest a = .4

With additional exact probabilities

bitest a = .4, detail

Exact test that the probability of success is 0.46, given 22 successes in 74 trials

bitesti 74 22 .46

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bitesti

Statistics > Summaries, tables, and tests > Classical tests of hypotheses > Binomial probability test calculator

Syntax

Binomial probability test

bitest
$$varname == \#_p [if] [in] [weight] [, \underline{d}etail]$$

Immediate form of binomial probability test

```
bitesti \#_N \#_{\text{succ}} \#_p [, \underline{\mathbf{d}}etail]
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by and collect are allowed with bitest; see [U] 11.1.10 Prefix commands.

fweights are allowed with bitest; see [U] 11.1.6 weight.

Option

Advanced

detail shows the probability of the observed number of successes, $k_{\rm obs}$; the probability of the number of successes on the opposite tail of the distribution that is used to compute the two-sided p-value, $k_{\rm opp}$; and the probability of the point next to $k_{\rm opp}$. This information can be safely ignored. See the technical note below for details.

Remarks and examples

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Remarks are presented under the following headings:

bitesti bitesti

bitest

Example 1

We test 15 university students for high levels of one measure of visual quickness which, from other evidence, we believe is present in 30% of the nonuniversity population. Included in our data is quick, taking on the values 1 ("success") or 0 ("failure") depending on the outcome of the test.

- . use https://www.stata-press.com/data/r18/quick
- . bitest quick == 0.3

Binomial probability test

Variable	N Obse	erved k E	xpected k	Assumed p	Observed p
quick	15	7	4.5	0.30000	0.46667
Pr(k >= 7) Pr(k <= 7)	= 0.131143 = 0.949987	-			
Pr(k <= 1 or	$k \ge 7) = 0.166410$	(two-side	d test)		

The first part of the output reveals that, assuming a true probability of success of 0.3, the expected number of successes is 4.5 and that we observed seven. Said differently, the assumed frequency under the null hypothesis H_0 is 0.3, and the observed frequency is 0.47.

The first line under the table is a one-sided test; it is the probability of observing seven or more successes conditional on p = 0.3. It is a test of H_0 : p = 0.3 versus the alternative hypothesis H_A : p > 0.3. Said in English, the alternative hypothesis is that more than 30% of university students score at high levels on this test of visual quickness. The p-value for this hypothesis test is 0.13.

The second line under the table is a one-sided test of H_0 versus the opposite alternative hypothesis $H_{\rm A}$: p < 0.3.

The third line is the two-sided test. It is a test of H_0 versus the alternative hypothesis H_A : $p \neq 0.3$.

□ Technical note

The p-value of a hypothesis test is the probability (calculated assuming H_0 is true) of observing any outcome as extreme or more extreme than the observed outcome, with extreme meaning in the direction of the alternative hypothesis. In example 1, the outcomes $k = 8, 9, \dots, 15$ are clearly "more extreme" than the observed outcome $k_{\rm obs} = 7$ when considering the alternative hypothesis H_A : $p \neq 0.3$. However, outcomes with only a few successes are also in the direction of this alternative hypothesis. For two-sided hypotheses, outcomes with k successes are considered "as extreme or more extreme" than the observed outcome k_{obs} if $\Pr(k) \leq \Pr(k_{\text{obs}})$. Here $\Pr(k=0)$ and $\Pr(k=1)$ are both less than Pr(k=7), so they are included in the two-sided p-value.

The detail option allows you to see the probability (assuming that H_0 is true) of the observed successes (k = 7) and the probability of the boundary point (k = 1) of the opposite tail used for the two-sided p-value.

. bitest quick == 0.3, detail Binomial probability test

Variable	N Obse	rved k	Expected k	Assumed p	Observed p
quick	15	7	4.5	0.30000	0.46667
Pr(k >= 7) Pr(k <= 7) Pr(k <= 1 or	= 0.131143 = 0.949987 k >= 7) = 0.166410	(one-sid	ed test)		
Pr(k == 7) Pr(k == 2) Pr(k == 1)	= 0.081130 = 0.091560 = 0.030520	•	d) e extreme)		

Also shown is the probability of the point next to the boundary point. This probability, namely, Pr(k=2) = 0.092, is certainly close to the probability of the observed outcome Pr(k=7) = 0.081, so some people might argue that k=2 should be included in the two-sided p-value. Statisticians (at least some we know) would reply that the p-value is a precisely defined concept and that this is an arbitrary "fuzzification" of its definition. When you compute exact p-values according to the precise definition of a p-value, your type I error is never more than what you say it is—so no one can criticize you for being anticonservative. Including the point k=2 is being overly conservative because it makes the p-value larger yet. But it is your choice; being overly conservative, at least in statistics, is always safe. Know that bitest and bitesti always keep to the precise definition of a p-value, so if you wish to include this extra point, you must do so by hand or by using the r() stored results; see Stored results below.

bitesti

▶ Example 2

The binomial test is a function of two statistics and one parameter: N, the number of observations; $k_{\rm obs}$, the number of observed successes; and p, the assumed probability of a success on a trial. For instance, in a city of N=2,500,000, we observe $k_{\rm obs}=36$ cases of a particular disease when the population rate for the disease is p=0.00001.

. bitesti 2500000 36 .00001 Binomial probability test

	N	Observed k	Expecte	ed k	Assumed p	Observed p
2,500,	000	36		25	0.00001	0.00001
Pr(k >=	36)	=	0.022458	(on	e-sided test)	
Pr(k <=	36)	=	0.985448	(on	e-sided test)	
Pr(k <=	14 or	k >= 36) =	0.034859	(tw	o-sided test)	

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Stored results

bitest and bitesti store the following in r():

```
Scalars
    r(N)
                           number N of trials
                           assumed probability p of success
    r(P_p)
    r(k)
                           observed number k of successes
    r(p_1)
                           lower one-sided p-value
                           upper one-sided p-value
    r(p_u)
    r(p)
                           two-sided p-value
                           opposite extreme k
    r(k_opp)
                           probability of observed k (detail only)
    r(P_k)
    r(P_oppk)
                           probability of opposite extreme k (detail only)
    r(k_nopp)
                           k next to opposite extreme (detail only)
                           probability of k next to opposite extreme (detail only)
    r(P_noppk)
```

Methods and formulas

Let N, $k_{\rm obs}$, and p be, respectively, the number of observations, the observed number of successes, and the assumed probability of success on a trial. The expected number of successes is Np, and the observed probability of success on a trial is $k_{\rm obs}/N$.

bitest and bitesti compute exact p-values based on the binomial distribution. The upper one-sided p-value is

$$\Pr(k \ge k_{\text{obs}}) = \sum_{m=k_{\text{obs}}}^{N} {N \choose m} p^m (1-p)^{N-m}$$

The lower one-sided p-value is

$$\Pr(k \le k_{\text{obs}}) = \sum_{m=0}^{k_{\text{obs}}} \binom{N}{m} p^m (1-p)^{N-m}$$

If $k_{\rm obs} \geq Np$, the two-sided p-value is

$$\Pr(k \le k_{\text{opp}} \text{ or } k \ge k_{\text{obs}})$$

where $k_{\rm opp}$ is the largest number $\leq Np$ such that $\Pr(k=k_{\rm opp}) \leq \Pr(k=k_{\rm obs})$. If $k_{\rm obs} < Np$, the two-sided p-value is

$$Pr(k \le k_{obs} \text{ or } k \ge k_{opp})$$

where k_{opp} is the smallest number $\geq Np$ such that $\Pr(k = k_{\text{opp}}) \leq \Pr(k = k_{\text{obs}})$.

Reference

Hoel, P. G. 1984. Introduction to Mathematical Statistics. 5th ed. New York: Wiley.

Also see

[R] ci — Confidence intervals for means, proportions, and variances

[R] **prtest** — Tests of proportions

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