

Mathematical functions

[Contents](#)[Functions](#)[Video example](#)[References](#)[Also see](#)

## Contents

<code>abs(<i>x</i>)</code>	the absolute value of <i>x</i>
<code>ceil(<i>x</i>)</code>	the unique integer <i>n</i> such that $n - 1 < x \leq n$ ; <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>ceil(.a) = .a</code>
<code>cloglog(<i>x</i>)</code>	the complementary log-log of <i>x</i>
<code>comb(<i>n</i>,<i>k</i>)</code>	the combinatorial function $n!/\{k!(n-k)!\}$
<code>digamma(<i>x</i>)</code>	the <code>digamma()</code> function, $d \ln \Gamma(x)/dx$
<code>exp(<i>x</i>)</code>	the exponential function $e^x$
<code>expm1(<i>x</i>)</code>	$e^x - 1$ with higher precision than <code>exp(<i>x</i>) - 1</code> for small values of $ x $
<code>floor(<i>x</i>)</code>	the unique integer <i>n</i> such that $n \leq x < n + 1$ ; <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>floor(.a) = .a</code>
<code>int(<i>x</i>)</code>	the integer obtained by truncating <i>x</i> toward 0 (thus, <code>int(5.2) = 5</code> and <code>int(-5.8) = -5</code> ); <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>int(.a) = .a</code>
<code>invcloglog(<i>x</i>)</code>	the inverse of the complementary log-log function of <i>x</i>
<code>invlogit(<i>x</i>)</code>	the inverse of the logit function of <i>x</i>
<code>ln(<i>x</i>)</code>	the natural logarithm, $\ln(x)$
<code>ln1m(<i>x</i>)</code>	the natural logarithm of $1 - x$ with higher precision than <code>ln(1 - <i>x</i>)</code> for small values of $ x $
<code>ln1p(<i>x</i>)</code>	the natural logarithm of $1 + x$ with higher precision than <code>ln(1 + <i>x</i>)</code> for small values of $ x $
<code>lnfactorial(<i>n</i>)</code>	the natural log of <i>n</i> factorial = $\ln(n!)$
<code>lngamma(<i>x</i>)</code>	$\ln\{\Gamma(x)\}$
<code>log(<i>x</i>)</code>	a synonym for <code>ln(<i>x</i>)</code>
<code>log10(<i>x</i>)</code>	the base-10 logarithm of <i>x</i>
<code>log1m(<i>x</i>)</code>	a synonym for <code>ln1m(<i>x</i>)</code>
<code>log1p(<i>x</i>)</code>	a synonym for <code>ln1p(<i>x</i>)</code>
<code>logit(<i>x</i>)</code>	the log of the odds ratio of <i>x</i> , $\text{logit}(x) = \ln\{x/(1-x)\}$
<code>max(<i>x</i><sub>1</sub>,<i>x</i><sub>2</sub>,...,<i>x</i><sub><i>n</i></sub>)</code>	the maximum value of <i>x</i> <sub>1</sub> , <i>x</i> <sub>2</sub> , ..., <i>x</i> <sub><i>n</i></sub>
<code>min(<i>x</i><sub>1</sub>,<i>x</i><sub>2</sub>,...,<i>x</i><sub><i>n</i></sub>)</code>	the minimum value of <i>x</i> <sub>1</sub> , <i>x</i> <sub>2</sub> , ..., <i>x</i> <sub><i>n</i></sub>
<code>mod(<i>x</i>,<i>y</i>)</code>	the modulus of <i>x</i> with respect to <i>y</i>
<code>reldif(<i>x</i>,<i>y</i>)</code>	the “relative” difference $ x - y /( y  + 1)$ ; 0 if both arguments are the same type of extended missing value; <i>missing</i> if only one argument is missing or if the two arguments are two different types of <i>missing</i>

## 2 Mathematical functions

---

<code>round(x, y)</code> or <code>round(x)</code>	$x$ rounded in units of $y$ or $x$ rounded to the nearest integer if the argument $y$ is omitted; $x$ (not “.”) if $x$ is missing (meaning that <code>round(.a) = .a</code> and that <code>round(.a, y) = .a</code> if $y$ is not missing) and if $y$ is missing, then “.” is returned
<code>sign(x)</code>	the sign of $x$ : $-1$ if $x < 0$ , $0$ if $x = 0$ , $1$ if $x > 0$ , or <i>missing</i> if $x$ is missing
<code>sqrt(x)</code>	the square root of $x$
<code>sum(x)</code>	the running sum of $x$ , treating missing values as zero
<code>trigamma(x)</code>	the second derivative of <code>lngamma(x) = d<sup>2</sup> lnΓ(x)/dx<sup>2</sup></code>
<code>trunc(x)</code>	a synonym for <code>int(x)</code>

## Functions

`abs(x)`

Description: the absolute value of  $x$

Domain:  $-8e+307$  to  $8e+307$

Range:  $0$  to  $8e+307$

`ceil(x)`

Description: the unique integer  $n$  such that  $n - 1 < x \leq n$ ;  $x$  (not “.”) if  $x$  is missing, meaning that `ceil(.a) = .a`

Also see `floor(x)`, `int(x)`, and `round(x)`.

Domain:  $-8e+307$  to  $8e+307$

Range: integers in  $-8e+307$  to  $8e+307$

`cloglog(x)`

Description: the complementary log-log of  $x$   
$$\text{cloglog}(x) = \ln\{-\ln(1-x)\}$$

Domain:  $0$  to  $1$

Range:  $-8e+307$  to  $8e+307$

`comb(n, k)`

Description: the combinatorial function  $n!/\{k!(n-k)!\}$

Domain  $n$ : integers  $1$  to  $1e+305$

Domain  $k$ : integers  $0$  to  $n$

Range:  $0$  to  $8e+307$  or *missing*

`digamma(x)`

Description: the `digamma()` function,  $d \ln \Gamma(x)/dx$

This is the derivative of `lngamma(x)`. The `digamma(x)` function is sometimes called the psi function,  $\psi(x)$ .

Domain:  $-1e+15$  to  $8e+307$

Range:  $-8e+307$  to  $8e+307$  or *missing*

**exp( $x$ )**

Description: the exponential function  $e^x$

This function is the inverse of `ln( $x$ )`. To compute  $e^x - 1$  with high precision for small values of  $|x|$ , use `expm1( $x$ )`.

Domain:  $-8e+307$  to  $709$

Range:  $0$  to  $8e+307$

**expm1( $x$ )**

Description:  $e^x - 1$  with higher precision than `exp( $x$ ) - 1` for small values of  $|x|$

Domain:  $-8e+307$  to  $709$

Range:  $-1$  to  $8e+307$

**floor( $x$ )**

Description: the unique integer  $n$  such that  $n \leq x < n + 1$ ;  $x$  (not “.”) if  $x$  is missing, meaning that `floor(.a) = .a`

Also see `ceil( $x$ )`, `int( $x$ )`, and `round( $x$ )`.

Domain:  $-8e+307$  to  $8e+307$

Range: integers in  $-8e+307$  to  $8e+307$

**int( $x$ )**

Description: the integer obtained by truncating  $x$  toward 0 (thus, `int(5.2) = 5` and `int(-5.8) = -5`);  $x$  (not “.”) if  $x$  is missing, meaning that `int(.a) = .a`

One way to obtain the closest integer to  $x$  is `int(x+sign( $x$ )/2)`, which simplifies to `int(x+0.5)` for  $x \geq 0$ . However, use of the `round()` function is preferred. Also see `round( $x$ )`, `ceil( $x$ )`, and `floor( $x$ )`.

Domain:  $-8e+307$  to  $8e+307$

Range: integers in  $-8e+307$  to  $8e+307$

**invcloglog( $x$ )**

Description: the inverse of the complementary log-log function of  $x$

$$\text{invcloglog}(x) = 1 - \exp\{-\exp(x)\}$$

Domain:  $-8e+307$  to  $8e+307$

Range:  $0$  to  $1$  or *missing*

**invlogit( $x$ )**

Description: the inverse of the logit function of  $x$

$$\text{invlogit}(x) = \exp(x) / \{1 + \exp(x)\}$$

Domain:  $-8e+307$  to  $8e+307$

Range:  $0$  to  $1$  or *missing*

**ln(x)**

Description: the natural logarithm,  $\ln(x)$

This function is the inverse of  $\exp(x)$ . The logarithm of  $x$  in base  $b$  can be calculated via  $\log_b(x) = \log_a(x)/\log_a(b)$ . Hence,

$$\log_5(x) = \ln(x)/\ln(5) = \log(x)/\log(5) = \log_{10}(x)/\log_{10}(5)$$

$$\log_2(x) = \ln(x)/\ln(2) = \log(x)/\log(2) = \log_{10}(x)/\log_{10}(2)$$

You can calculate  $\log_b(x)$  by using the formula that best suits your needs. To compute  $\ln(1-x)$  and  $\ln(1+x)$  with high precision for small values of  $|x|$ , use **ln1m(x)** and **ln1p(x)**, respectively.

Domain:  $1e-323$  to  $8e+307$

Range:  $-744$  to  $709$

**ln1m(x)**

Description: the natural logarithm of  $1-x$  with higher precision than  $\ln(1-x)$  for small values of  $|x|$

Domain:  $-8e+307$  to  $1 - \text{c(epsdouble)}$

Range:  $-37$  to  $709$

**ln1p(x)**

Description: the natural logarithm of  $1+x$  with higher precision than  $\ln(1+x)$  for small values of  $|x|$

Domain:  $-1 + \text{c(epsdouble)}$  to  $8e+307$

Range:  $-37$  to  $709$

**lnfactorial(n)**

Description: the natural log of  $n$  factorial =  $\ln(n!)$

To calculate  $n!$ , use `round(exp(lnfactorial(n)),1)` to ensure that the result is an integer. Logs of factorials are generally more useful than the factorials themselves because of overflow problems.

Domain: integers  $0$  to  $1e+305$

Range:  $0$  to  $8e+307$

**lngamma(x)**

Description:  $\ln\{\Gamma(x)\}$

Here the gamma function,  $\Gamma(x)$ , is defined by  $\Gamma(x) = \int_0^\infty t^{x-1}e^{-t}dt$ . For integer values of  $x > 0$ , this is  $\ln((x-1)!)$ .

**lngamma(x)** for  $x < 0$  returns a number such that  $\exp(\text{lngamma}(x))$  is equal to the absolute value of the gamma function,  $\Gamma(x)$ . That is, **lngamma(x)** always returns a real (not complex) result.

Domain:  $-2,147,483,648$  to  $1e+305$  (excluding negative integers)

Range:  $-8e+307$  to  $8e+307$

**log(x)**

Description: a synonym for **ln(x)**

$\log_{10}(x)$

Description: the base-10 logarithm of  $x$

Domain:  $1e-323$  to  $8e+307$

Range:  $-323$  to  $308$

$\log_{1m}(x)$

Description: a synonym for  $\ln_{1m}(x)$

$\log_{1p}(x)$

Description: a synonym for  $\ln_{1p}(x)$

$\logit(x)$

Description: the log of the odds ratio of  $x$ ,  $\logit(x) = \ln\{x/(1-x)\}$

Domain: 0 to 1 (exclusive)

Range:  $-8e+307$  to  $8e+307$  or *missing*

$\max(x_1, x_2, \dots, x_n)$

Description: the maximum value of  $x_1, x_2, \dots, x_n$

Unless all arguments are *missing*, missing values are ignored.

$\max(2, 10, ., 7) = 10$

$\max(., ., .) = .$

Domain  $x_1$ :  $-8e+307$  to  $8e+307$  or *missing*

Domain  $x_2$ :  $-8e+307$  to  $8e+307$  or *missing*

...

Domain  $x_n$ :  $-8e+307$  to  $8e+307$  or *missing*

Range:  $-8e+307$  to  $8e+307$  or *missing*

$\min(x_1, x_2, \dots, x_n)$

Description: the minimum value of  $x_1, x_2, \dots, x_n$

Unless all arguments are *missing*, missing values are ignored.

$\min(2, 10, ., 7) = 2$

$\min(., ., .) = .$

Domain  $x_1$ :  $-8e+307$  to  $8e+307$  or *missing*

Domain  $x_2$ :  $-8e+307$  to  $8e+307$  or *missing*

...

Domain  $x_n$ :  $-8e+307$  to  $8e+307$  or *missing*

Range:  $-8e+307$  to  $8e+307$  or *missing*

**mod**( $x, y$ )Description: the modulus of  $x$  with respect to  $y$ 

$$\text{mod}(x, y) = x - y \text{ floor}(x/y)$$

$$\text{mod}(x, 0) = .$$

Domain  $x$ :  $-8\text{e}+307$  to  $8\text{e}+307$ Domain  $y$ : 0 to  $8\text{e}+307$ Range: 0 to  $8\text{e}+307$ **reldif**( $x, y$ )Description: the “relative” difference  $|x - y|/(|y| + 1)$ ; 0 if both arguments are the same type of extended missing value; *missing* if only one argument is missing or if the two arguments are two different types of *missing*Domain  $x$ :  $-8\text{e}+307$  to  $8\text{e}+307$  or *missing*Domain  $y$ :  $-8\text{e}+307$  to  $8\text{e}+307$  or *missing*Range: 0 to  $8\text{e}+307$  or *missing***round**( $x, y$ ) or **round**( $x$ )Description:  $x$  rounded in units of  $y$  or  $x$  rounded to the nearest integer if the argument  $y$  is omitted;  $x$  (not “.”) if  $x$  is missing (meaning that  $\text{round}(.a) = .a$  and that  $\text{round}(.a, y) = .a$  if  $y$  is not missing) and if  $y$  is missing, then “.” is returned

For  $y = 1$ , or with  $y$  omitted, this amounts to the closest integer to  $x$ ;  $\text{round}(5.2, 1)$  is 5, as is  $\text{round}(4.8, 1)$ ;  $\text{round}(-5.2, 1)$  is  $-5$ , as is  $\text{round}(-4.8, 1)$ . The rounding definition is generalized for  $y \neq 1$ . With  $y = 0.01$ , for instance,  $x$  is rounded to two decimal places;  $\text{round}(\text{sqrt}(2), .01)$  is 1.41.  $y$  may also be larger than 1;  $\text{round}(28, 5)$  is 30, which is 28 rounded to the closest multiple of 5. For  $y = 0$ , the function is defined as returning  $x$  unmodified.

For values of  $x$  exactly at midpoints, where it may not be clear whether to round up or down,  $x$  is always rounded up to the larger value. For example,  $\text{round}(4.5)$  is 5 and  $\text{round}(-4.5)$  is  $-4$ . Note that rounding a number is based on the floating-point number representation of the number instead of the number itself. So  $\text{round}()$  is sensitive to representation errors and precision limits. For example, 0.15 has no exact floating-point number representation. Therefore,  $\text{round}(0.15, 0.1)$  is 0.1 instead of 0.2. See [U] [13.12 Precision and problems therein](#) for details.

Also see  $\text{int}(x)$ ,  $\text{ceil}(x)$ , and  $\text{floor}(x)$ .

Domain  $x$ :  $-8\text{e}+307$  to  $8\text{e}+307$ Domain  $y$ :  $-8\text{e}+307$  to  $8\text{e}+307$ Range:  $-8\text{e}+307$  to  $8\text{e}+307$ **sign**( $x$ )Description: the sign of  $x$ :  $-1$  if  $x < 0$ , 0 if  $x = 0$ , 1 if  $x > 0$ , or *missing* if  $x$  is missingDomain:  $-8\text{e}+307$  to  $8\text{e}+307$  or *missing*Range:  $-1, 0, 1$  or *missing*

**sqrt(*x*)**

Description: the square root of *x*

Domain: 0 to 8e+307

Range: 0 to 1e+154

**sum(*x*)**

Description: the running sum of *x*, treating missing values as zero

For example, following the command `generate y=sum(x)`, the *j*th observation on *y* contains the sum of the first through *j*th observations on *x*. See [D] [egen](#) for an alternative sum function, `total()`, that produces a constant equal to the overall sum.

Domain: all real numbers or *missing*

Range:  $-8e+307$  to  $8e+307$  (excluding *missing*)

**trigamma(*x*)**

Description: the second derivative of  $\text{lngamma}(x) = d^2 \ln \Gamma(x) / dx^2$

The `trigamma()` function is the derivative of `digamma(x)`.

Domain:  $-1e+15$  to  $8e+307$

Range: 0 to  $8e+307$  or *missing*

**trunc(*x*)**

Description: a synonym for `int(x)`

## Video example

[How to round a continuous variable](#)

## References

- Abramowitz, M., and I. A. Stegun, ed. 1964. *Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables*. Washington, DC: National Bureau of Standards.
- Cox, N. J. 2003. *Stata tip 2: Building with floors and ceilings*. *Stata Journal* 3: 446–447.
- . 2007. *Stata tip 43: Remainders, selections, sequences, extractions: Uses of the modulus*. *Stata Journal* 7: 143–145.
- . 2018. *Speaking Stata: From rounding to binning*. *Stata Journal* 18: 741–754.
- Oldham, K. B., J. C. Myland, and J. Spanier. 2009. *An Atlas of Functions*. 2nd ed. New York: Springer.

## Also see

[FN] [Functions by category](#)

[D] [egen](#) — Extensions to generate

[D] [generate](#) — Create or change contents of variable

[M-4] [Intro](#) — Categorical guide to Mata functions

[U] [13.3 Functions](#)

Stata, Stata Press, and Mata are registered trademarks of StataCorp LLC. Stata and Stata Press are registered trademarks with the World Intellectual Property Organization of the United Nations. StataNow and NetCourseNow are trademarks of StataCorp LLC. Other brand and product names are registered trademarks or trademarks of their respective companies. Copyright © 1985–2023 StataCorp LLC, College Station, TX, USA. All rights reserved.



For suggested citations, see the [FAQ on citing Stata documentation](#).