bayes: xtnbreg — Bayesian random-effects negative binomial model

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# Description

Title

**bayes:** xtnbreg fits a Bayesian panel-data random-effects negative binomial model to a nonnegative count outcome; see [BAYES] **bayes** and [XT] **xtnbreg** for details.

# Quick start

- Bayesian random-effects negative binomial model of y on x1 and x2 with random intercepts by id (after xtseting on panel variable id), using default normal priors for regression coefficients and beta prior for the random effects, and Pareto prior for the shape parameters of the beta prior bayes: xtnbreg y x1 x2
- Use a standard deviation of 10 instead of 100 for the default normal priors bayes, normalprior(10): xtnbreg y x1 x2

Use uniform priors for the slopes and a normal prior for the intercept bayes, prior({y: x1 x2}, uniform(-10,10)) /// prior({y:\_cons}, normal(0,10)): xtnbreg y x1 x2

- Save simulation results to simdata.dta, and use a random-number seed for reproducibility bayes, saving(simdata) rseed(123): xtnbreg y x1 x2
- Specify 20,000 Markov chain Monte Carlo (MCMC) samples, set length of the burn-in period to 5,000, and request that a dot be displayed every 500 simulations bayes, mcmcsize(20000) burnin(5000) dots(500): xtnbreg y x1 x2
- In the above, request that the 90% highest posterior density (HPD) credible interval be displayed instead of the default 95% equal-tailed credible interval bayes, clevel(90) hpd
- Display incidence-rate ratios instead of coefficients bayes: xtnbreg y x1 x2, irr

Display incidence-rate ratios on replay bayes, irr

Random-effects model with exposure variable evar bayes: xtnbreg y x1 x2, exposure(evar)

Also see Quick start in [BAYES] bayes and Quick start in [XT] xtnbreg.

### Menu

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## **Syntax**

bayes [, bayesopts]: xtnbreg depvar [indepvars] [if] [in] [, options]

options	Description
Model	
<u>nocons</u> tant	suppress constant term
$exposure(varname_e)$	include $\ln(varname_e)$ in model with coefficient constrained to 1
$\overline{off}set(varname_o)$	include $varname_o$ in model with coefficient constrained to 1
Reporting	
<u>ir</u> r	report incidence-rate ratios
display_options	control spacing, line width, and base and empty cells
<u>l</u> evel(#)	set credible level; default is level(95)

A panel variable must be specified; see [XT] xtset.

*indepvars* may contain factor variables; see [U] **11.4.3 Factor variables**. *depvar, indepvars, varname<sub>e</sub>, and varname<sub>o</sub> may contain time-series operators; see [U]* **11.4.4 Time-series varlists**. bayes: xtnbreg, level() is equivalent to bayes, clevel(): xtnbreg. For a detailed description of options, see *Options for RE/FE models* in [XT] **xtnbreg**.

bayesopts	Description
Priors	
* <u>normalpr</u> ior(#)	specify standard deviation of default normal priors for regression coefficients; default is normalprior(100)
prior( <i>priorspec</i> )	prior for model parameters; this option may be repeated
dryrun	show model summary without estimation
Simulation	
nchains(#)	number of chains; default is to simulate one chain
<pre>mcmcsize(#)</pre>	MCMC sample size; default is mcmcsize(10000)
<pre>burnin(#)</pre>	burn-in period; default is burnin(2500)
<u>thin</u> ning(#)	thinning interval; default is thinning(1)
rseed(#)	random-number seed
<pre>exclude(paramref)</pre>	specify model parameters to be excluded from the simulation results
Blocking	
<pre>block(paramref[, blockopts])</pre>	specify a block of model parameters; this option may be repeated
blocksummary	display block summary

Initialization	
<pre>initial(initspec)</pre>	specify initial values for model parameters with a single chain
init#(initspec)	specify initial values for #th chain; requires nchains()
initall( <i>initspec</i> )	specify initial values for all chains; requires nchains()
nomleinitial	suppress the use of maximum likelihood estimates as starting values
initrandom	specify random initial values
initsummary	display initial values used for simulation
* <u>noi</u> sily	display output from the estimation command during initialization
Adaptation	
adaptation( <i>adaptopts</i> )	control the adaptive MCMC procedure
<u>sc</u> ale(#)	initial multiplier for scale factor; default is scale(2.38)
<pre>covariance(cov)</pre>	initial proposal covariance; default is the identity matrix
Reporting	
<u>clev</u> el(#)	set credible interval level; default is clevel(95)
hpd	display HPD credible intervals instead of the default equal-tailed credible intervals
* <u>ir</u> r	report incidence-rate ratios
<u>ef</u> orm[( <i>string</i> )]	report exponentiated coefficients and, optionally, label as string
remargl	compute log marginal-likelihood; suppressed by default
batch(#)	specify length of block for batch-means calculations; default is batch(0)
<pre>saving(filename[, replace])</pre>	save simulation results to <i>filename</i> .dta
nomodelsummary	suppress model summary
chainsdetail	display detailed simulation summary for each chain
[no]dots	suppress dots or display dots every 100 iterations and iteration numbers every 1,000 iterations; default is nodots
dots(# $[, every(#)]$ )	display dots as simulation is performed
[no]show(paramref)	specify model parameters to be excluded from or included in the output
$\underline{\text{showre}} ffects [(reref)]$	specify that all or a subset of random-effects parameters be included in the output
<u>notab</u> le	suppress estimation table
<u>nohead</u> er	suppress output header
<pre>title(string)</pre>	display string as title above the table of parameter estimates
display_options	control spacing, line width, and base and empty cells
Advanced	
<pre>search(search_options)</pre>	control the search for feasible initial values
corrlag(#)	specify maximum autocorrelation lag; default varies
corrtol(#)	specify autocorrelation tolerance; default is corrtol(0.01)

\*Starred options are specific to the bayes prefix; other options are common between bayes and bayesmh. Options prior() and block() may be repeated.

priorspec and paramref are defined in [BAYES] bayesmh.

paramref may contain factor variables; see [U] 11.4.3 Factor variables.

collect is allowed; see [U] 11.1.10 Prefix commands.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

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Model parameters are regression coefficients {*depvar:indepvars*}, random effects {U[*panelvar*]} or simply {U}, and shape parameters {**r**} and {**s**} for the beta prior of {U}; also see *Methods and formulas*. Use the dryrun option to see the definitions of model parameters prior to estimation.

For a detailed description of bayesopts, see Options in [BAYES] bayes.

## **Remarks and examples**

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For a general introduction to Bayesian analysis, see [BAYES] **Intro**. For a general introduction to Bayesian estimation using an adaptive Metropolis–Hastings algorithm, see [BAYES] **bayesmh**. For remarks and examples specific to the **bayes** prefix, see [BAYES] **bayes**. For details about the estimation command, see [XT] **xtnbreg**.

For a simple example of the bayes prefix, see *Introductory example* in [BAYES] bayes. Also see *Panel-data models* in [BAYES] bayes.

### Stored results

See Stored results in [BAYES] bayes. In addition, bayes: xtnbreg also stores the following results:

Macros e(ivar) variable denoting groups e(redistrib) distribution of random effects

### Methods and formulas

Bayesian random-effects negative binomial models are based on random-effects negative binomial models described in *Methods and formulas* of [XT] **xtnbreg**.

Let  $y_{it}$  be the count for the *t*th observation in the *i*th group. We assume  $y_{it} | \gamma_{it} \sim \text{Poisson}(\gamma_{it})$ , where  $\gamma_{it} | u_i \sim \text{gamma}\{\lambda_{it}, (1 - u_i)/u_i\}$  with  $\lambda_{it} = \exp(\mathbf{x}_{it}\beta + \text{offset}_{it})$  and  $u_i$  is a dispersioncontrol parameter that varies randomly across groups. The likelihood of the model is thus

$$\Pr(Y_{it} = y_{it} \mid \mathbf{x}_{it}, u_i) = \frac{\Gamma(\lambda_{it} + y_{it})}{\Gamma(\lambda_{it})\Gamma(y_{it} + 1)} u_i^{\lambda_{it}} (1 - u_i)^{y_{it}}$$

We further assume that random-effects dispersion parameters  $u_i$ 's are a priori independent and follow beta distribution with shape parameters r and s,  $u_i \sim \text{Beta}(r, s)$ . The hyperprior for the shape parameters is chosen so that the joint distribution of the mean r/(r+s) and inverse square-root of the sample size (r+s) of the beta distribution is uniform,  $\{r/(r+s), (r+s)^{-0.5}\} \sim 1$ ; see Gelman et al. (2014, sec. 5.3). This choice leads to a diffused distribution for (r, s) with a density proportional to  $(r+s)^{-2.5}$ , which is a Pareto-type distribution.

bayes: xtnbreg uses the default initial value of 0.5 for the random effects  $u_i$ 's.

See Methods and formulas in [BAYES] bayesmh.

### Reference

Gelman, A., J. B. Carlin, H. S. Stern, D. B. Dunson, A. Vehtari, and D. B. Rubin. 2014. *Bayesian Data Analysis*. 3rd ed. Boca Raton, FL: Chapman and Hall/CRC.

## Also see

[BAYES] **bayes** — Bayesian regression models using the bayes prefix<sup>+</sup>

- [XT] **xtnbreg** Fixed-effects, random-effects, & population-averaged negative binomial models
- [BAYES] Bayesian postestimation Postestimation tools for bayesmh and the bayes prefix
- [BAYES] Bayesian estimation Bayesian estimation commands
- [BAYES] Bayesian commands Introduction to commands for Bayesian analysis
- [BAYES] Intro Introduction to Bayesian analysis

[BAYES] Glossary

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